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Strong correlations generically protect *d*-wave superconductivity against disorder

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We address the question of why strongly correlated *d*-wave superconductors, such as the cuprates, prove to be surprisingly robust against the introduction of nonmagnetic impurities. We show that, very generally, both the pair-breaking and the normal state transport scattering rates are significantly suppressed by strong correlations effects arising in the proximity to a Mott insulating state. We also show that the correlation-renormalized scattering amplitude is generically enhanced in the forward direction, an effect which was previously often ascribed to the specific scattering by charged impurities outside the copper-oxide planes.

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Introduction. For many classes of unconventional superconductors, such as the cuprates [1–4], heavy fermion superconductors [5], organic materials [6,7], and iron pnictides [8], electronic interactions are believed to be essential. Among the many puzzling features of these systems is their behavior in the presence of disorder [9,10]. In weakly interacting *d*-wave superconductors, Abrikosov-Gor'kov (AG) theory predicts that a small concentration of nonmagnetic impurities should bring the transition temperature T_c to zero. In the case of the cuprates, however, experiments have shown that these *d*-wave superconductors are very robust against disorder [3,11–13]. This feature was frequently ascribed to scattering by charged off-plane impurities, which is mostly in the forward direction (see, e.g., [14]). It has also been attributed to the frequency dependence of the pairing interactions in spin-fluctuation theories [15]. The puzzle was partially clarified, however, once strong electronic interactions were shown to give rise to the impurity screening effects seen in these experiments, especially as captured by the Gutzwiller-projected wave function [16–24]. Despite this progress, it would be desirable to understand both qualitatively and quantitatively whether disorder screening has any significant influence on T_c as well as on the normal state transport properties. In other words, can a physically transparent answer be given to the following question: how do strong correlations and Mott physics affect the predictions of AG theory?

The transition temperature in the underdoped region of the hole-doped cuprates is believed to be influenced by phase fluctuations, various types of competing orders (such as charge- and spin-density waves), stripe formation, etc. Consequently, impurities act as nucleation centers, which complicates the analysis considerably. In the overdoped region, however, T_c is dominated by the superconducting gap opening, thus offering a particularly favorable window into the interplay between disorder and interactions. This regime will be the focus of the present work.

In the presence of impurities, the strongly correlated state readjusts itself and creates a renormalized disorder potential. In the dilute limit, the AG theory can be extended to describe the effect of this renormalized potential on T_c degradation and transport properties. We will describe in this paper how electronic interactions lead to a much slower decrease of T_c as compared to the weak-coupling theory. Our results demonstrate that (i) this effect is intrinsically tied to the proximity to

the Mott insulating state, although it is significant even above optimal doping, (ii) the doping dependence of normal state resistivity is different from that of the pair-breaking scattering rate, which governs T_c , and (iii) the softening of the disorder potential by interactions leads to a strong enhancement of the forward scattering amplitude.

Model and method. We start with the *t*-*J* model on a cubic lattice in *d* dimensions with dilute nonmagnetic impurities

$$H = -t \sum_{\langle ij \rangle \sigma} c_{i\sigma}^\dagger c_{j\sigma} + J \sum_{\langle ij \rangle} \mathbf{S}_i \cdot \mathbf{S}_j + \sum_i (\epsilon_i - \mu_0) n_i, \quad (1)$$

where $c_{i\sigma}^\dagger$ ($c_{i\sigma}$) is the creation (annihilation) operator of an electron with spin projection σ on site *i*, *t* is the hopping matrix element between nearest neighbors, *J* is the superexchange coupling constant between nearest-neighbor sites, $n_i = \sum_\sigma c_{i\sigma}^\dagger c_{i\sigma}$ is the number operator, and μ_0 is the chemical potential. The no-double-occupancy constraint ($n_i \leq 1$) is implied. We work in units such that $\hbar = k_B = a = 1$, where *a* is the lattice spacing and the total number of lattice sites is *V*. For definiteness, we will set $J = t/3$. The impurities are taken into account through a random on-site potential described by ϵ_i . We use a model of disorder in which we set the potential $\epsilon_i = t$ and randomly place the impurities on lattice sites with *n* impurities per unit volume and no correlations between their positions. Note that this model assumes random nonmagnetic scattering but does not describe the removal of magnetic ions. We will focus on the two-dimensional case relevant to the cuprates, but our results are easily generalizable to higher dimensions with few modifications.

We proceed with *U*(1) slave boson theory, the details of which can be found in [4,25–28]. Briefly, it starts with the replacement $c_{i\sigma}^\dagger \rightarrow f_{i\sigma}^\dagger b_i$, where $f_{i\sigma}^\dagger$ and b_i are auxiliary fermionic (spinon) and bosonic (slave boson) fields. This substitution is faithful if the constraint $n_i \leq 1$ is replaced by $\sum_\sigma f_{i\sigma}^\dagger f_{i\sigma} + b_i^\dagger b_i = 1$. The latter is enforced through Lagrange multiplier fields λ_i on each site. The *J* term is then decoupled through additional Hubbard-Stratonovich bosonic fields in the particle-particle (Δ_{ij}) and particle-hole (χ_{ij}) channels. The auxiliary bosonic fields are all treated in the saddle-point approximation, which here is *spatially inhomogeneous* due to the presence of disorder: $\langle b_i \rangle = r_i$, which governs the local quasiparticle residue $Z_i = r_i^2$, $\langle \lambda_i \rangle$ (we will denote it simply by λ_i), which renormalizes the site

energies, and $\chi_{ij} = \sum_{\sigma} \langle f_{i\sigma}^{\dagger} f_{j\sigma} \rangle$ and $\Delta_{ij} = \langle f_{i\uparrow} f_{j\downarrow} - f_{i\downarrow} f_{j\uparrow} \rangle$, which describe, respectively, the strength of a spinon singlet and the pairing amplitude across the corresponding bonds. We also made the change $J \rightarrow \tilde{J} = \frac{3}{8}J$. This choice is made so that the saddle-point approximation of the above multichannel Hubbard-Stratonovitch transformation coincides with the mean-field results [4]. We note, however, that the usual choice $\tilde{J} = \frac{1}{4}J$ would give rise to hardly noticeable changes in the numerical results. We stress that the f electrons mentioned throughout the text are only auxiliary fermions, usually called spinons, rather than the physical electrons. They are related at the saddle point by $c_{i\sigma}^{\dagger} = r_i f_{i\sigma}^{\dagger}$. Note that the nontrivial effects of this work come from the self-consistent spatial readjustments of the condensed fields to the disorder potential.

In the clean limit ($\epsilon_i = 0$) and in the saddle-point approximation, the bosonic fields are spatially uniform: $r_i = r_0$, $\lambda_i = \lambda_0$, $\chi_{ij} = \chi \Gamma_s(i, j)$, and $\Delta_{ij} = \Delta_0 \Gamma_d(i, j)$. Here, $\Gamma_{s,d}(i, j)$ are the real space cubic harmonics which, in \mathbf{k} space, are given by $\Gamma_s(\mathbf{k}) = 2(\cos k_x + \cos k_y)$ and $\Gamma_d(\mathbf{k}) = 2(\cos k_x - \cos k_y)$. As the doping level (measured with respect to half-filling) $x = 1 - \sum_i n_i / V = r_0^2$ is increased, the slave boson condensation temperature T_b increases monotonically from zero, whereas the Δ field condenses at a transition temperature T_{Δ} which decreases monotonically from a finite value at $x = 0$ to zero at an upper doping level x_{\max} [4,27]. The two curves meet at optimal doping x_{opt} . The dome below the two curves is the superconducting dome. Our focus in this paper is on the overdoped region $x > x_{\text{opt}}$, in which the superconducting transition temperature $T_c = T_{\Delta} < T_b$.

Within this spatially inhomogeneous theory, we are able to perform a complete quantitative calculation of the *effective* disorder potential. Details have been explained elsewhere [24]. Here, we will focus on the effects of disorder on the superconducting transition temperature T_c and on transport properties in the correlated normal state for $T \gtrsim T_c$ in the overdoped region. For this purpose, we can set $\Delta_{ij} = 0$. Moreover, in this range of temperature and dopings the other bosons, r_i , λ_i , and χ_{ij} , are thoroughly condensed and therefore fairly insensitive to finite temperature effects. We are thus justified in approximating them by their zero-temperature values.

We will focus on the case of weak scattering by dilute impurities $n \ll 1$, where a linear response theory is sufficient. In other words, we calculate the spatial fluctuations of the various condensed fields to first order in the perturbing potential ϵ_i [24]. Extensive numerical calculations carried out both in the normal and in the superconducting states have shown that the crucial spatial fluctuations come from the λ_i and r_i fields, whereas fluctuations of χ_{ij} play only a negligible role [24]. We will thus simply fix χ_{ij} at its clean limit value χ while allowing for the full self-consistent spatial adjustment of the λ_i and r_i fields to the disordered situation.

Given this setup, the superconducting transition at T_c corresponds to the formation of the order parameter $\Delta_{ij} = \langle f_{i\uparrow} f_{j\downarrow} - f_{i\downarrow} f_{j\uparrow} \rangle$. The condensing f electrons, on the other hand, are governed, in the clean limit by a dispersion relation renormalized by the slave boson fields r_0 and χ , $\tilde{h}(\mathbf{k}) \equiv -(tx + \tilde{J}\chi)\Gamma_s(\mathbf{k})$ and a renormalized chemical potential $\mu_0 - \lambda_0 \equiv -v_0$. This theory, therefore, describes a BCS-type

condensation of the f electrons. In the presence of disorder, the various fields will readjust themselves. The effect of dilute identical nonmagnetic impurities on T_c will therefore be captured within the Abrikosov-Gor'kov (AG) theory [29]. In that theory, the only input needed is the scattering T matrix due to a *single* impurity. For that purpose, we place a single impurity at the lattice origin $\epsilon_i = t\delta_{i,0}$. Crucially, however, the λ_i and r_i fields will differ from their clean-limit value inside an extended region around the impurity, not only at the origin. The effective T matrix will thus reflect this nontrivial rearrangement. As shown in Ref. [24], the impurity potential is “healed” within a length scale of a few lattice parameters, the so-called healing length. Furthermore, it was shown that the healing process/length is strongly influenced by electronic correlations and “Mottness,” even up to dopings $x \approx 0.3$. Therefore, as will be shown, the effective scattering will be strongly suppressed relative to the noncorrelated case.

We also look at the transport properties in the normal state around T_c . Again, the AG analysis can be straightforwardly applied in our case. The relevant input for the calculation of the resistivity is the *physical electron* scattering T matrix for a single impurity.

A straightforward calculation up to first order in the impurity potential gives the T matrix in momentum space for f fermions and physical (e) electrons, respectively, as (see Supplemental Material [30])

$$\begin{aligned} \langle \mathbf{k} | T^f | \mathbf{k}' \rangle &= xt \left[\frac{h(\mathbf{k}) + h(\mathbf{k}') - \Pi(\mathbf{k}' - \mathbf{k})}{\lambda_0 - \frac{\lambda_0}{2d} \Gamma_s(\mathbf{k}' - \mathbf{k}) - x \Pi(\mathbf{k}' - \mathbf{k})} \right], \quad (2) \\ \langle \mathbf{k} | T^e | \mathbf{k}' \rangle &= -t \left\{ \frac{\Pi(\mathbf{k}' - \mathbf{k}) + \frac{2v_0}{x} + \frac{\tilde{J}\chi}{tx} [h(\mathbf{k}) + h(\mathbf{k}')] }{\lambda_0 - \frac{\lambda_0}{2d} \Gamma_s(\mathbf{k}' - \mathbf{k}) - x \Pi(\mathbf{k}' - \mathbf{k})} \right\}, \quad (3) \end{aligned}$$

where $h(\mathbf{k}) = -t\Gamma_s(\mathbf{k})$ is the bare energy dispersion,

$$\Pi(\mathbf{k}) \equiv \frac{1 + \Pi^b(\mathbf{k})}{\Pi^a(\mathbf{k})}, \quad (4)$$

with

$$\begin{aligned} \Pi^a(\mathbf{k}) &= \frac{1}{V} \sum_{\mathbf{q}} \frac{f[\tilde{h}(\mathbf{q} + \mathbf{k})] - f[\tilde{h}(\mathbf{q})]}{\tilde{h}(\mathbf{q} + \mathbf{k}) - \tilde{h}(\mathbf{q})}, \\ \Pi^b(\mathbf{k}) &= \frac{1}{V} \sum_{\mathbf{q}} \frac{f[\tilde{h}(\mathbf{q} + \mathbf{k})] - f[\tilde{h}(\mathbf{q})]}{\tilde{h}(\mathbf{q} + \mathbf{k}) - \tilde{h}(\mathbf{q})} [h(\mathbf{q} + \mathbf{k}) + h(\mathbf{q})], \end{aligned}$$

and $f(x)$ is the Fermi-Dirac function at $T = 0$.

In order to assess the role of electronic correlations we will compare our full results as described above with a corresponding noncorrelated system in which $J = 0$. In the latter case, the T matrix is given simply by the lattice Fourier transform of the bare disorder potential, $\langle \mathbf{k} | T_0 | \mathbf{k}' \rangle = \epsilon(\mathbf{k}' - \mathbf{k}) = t$, and there is no distinction between auxiliary and physical fermions. The two sets of results will be called correlated and noncorrelated, respectively. Even at this point, the renormalizations due to strong correlations are clear: the \mathbf{k} -dependent factors in Eqs. (2) and (3), which reflect the spatial readjustments of the r_i and λ_i fields, make the bare potential “softer” and more nonlocal. Note also the extra x factor in Eq. (2) as compared to Eq. (3).

At low temperatures, only scattering very close to the Fermi level is relevant. We will thus calculate the T matrices at the Fermi surface. Furthermore, we are interested in the overdoped region, where the Fermi surface anisotropy becomes increasingly less pronounced as the doping increases. Therefore, we will simplify the actual lattice dispersion in favor of an isotropic one corresponding to the continuum limit, $h(\mathbf{k}) \approx -4t + tk^2$. This is equivalent to a bare effective mass $m = 1/2t$ and a renormalized one $m^* \equiv 1/(2tx + 2\tilde{J}\chi)$. Finally, we call E_F and k_F the Fermi energy and momentum for the bare dispersion $h(\mathbf{k})$, respectively, while $\tilde{E}_F = \frac{m^*}{m} E_F$ is the Fermi energy for the renormalized dispersion of the f fermions.

Pair breaking parameter. Once the scattering matrix has been determined, it is a trivial matter to write down the predictions of the Abrikosov-Gor'kov (AG) theory for the suppression of the superconducting transition temperature T_c (see Supplemental Material [30])

$$\ln \frac{T_{c0}}{T_c} = \psi\left(\frac{1}{2} + \frac{\alpha}{2}\right) - \psi\left(\frac{1}{2}\right), \quad (5)$$

where T_{c0} is the transition temperature in clean limit, $\alpha \equiv 1/(2\pi T_c \tau_{pb})$, and τ_{pb} is the pair breaking scattering time. The latter is given in the continuum limit by

$$\frac{1}{\tau_{pb}} = \frac{x^2 nm^*}{2\pi} \int_0^{2\pi} d\theta g\left[\left|\sin\left(\frac{\theta}{2}\right)\right|\right] (1 - \cos 2\theta), \quad (6)$$

where

$$g(y) \equiv \frac{t^2}{\{\rho^* \lambda_0 k_F^2 y^2 g_L(y) + x[1 - 2\rho^* E_F g_L(y)]\}^2}, \quad (7)$$

where $\rho^* = \frac{m^*}{2\pi}$ is the renormalized density of states and

$$g_L(y) \equiv \begin{cases} 1, & y \leq 1, \\ 1 - \sqrt{1 - y^{-2}}, & y > 1. \end{cases} \quad (8)$$

The factor of $1 - \cos 2\theta$ comes from the vertex corrections for d -wave pairing and can be generalized to other pairing symmetries by changing $\cos 2\theta$ to the corresponding lattice harmonic. The leading behavior for low impurity concentrations is

$$T_c = T_{c0} - \pi/8\tau_{pb}. \quad (9)$$

Figure 1 shows the ratio of the pair-breaking scattering rate $1/\tau_{pb}$ in the correlated case to the noncorrelated one. Note that, for the noncorrelated case,

$$\frac{1}{\tau_0} = \frac{nm}{2\pi} \int_0^{2\pi} d\theta t^2 (1 - \cos 2\theta) = nmt^2. \quad (10)$$

Clearly, pair breaking is strongly suppressed by electronic correlations. While this suppression is enhanced as the density-driven Mott transition is approached ($x \rightarrow 0$), it is still quite significant up to dopings of $x \approx 0.3$. As a result, the T_c degradation is expected to be considerably slower in that case and we expect the d -wave superconductivity to be more robust than predicted by the weak coupling theory. Equivalently, the critical impurity concentration n_c at which T_c vanishes is enhanced when compared to the noncorrelated case, 5–10 times in the range of dopings from 0.15 to 0.3. We note that this suppression of pair breaking by the impurities is completely

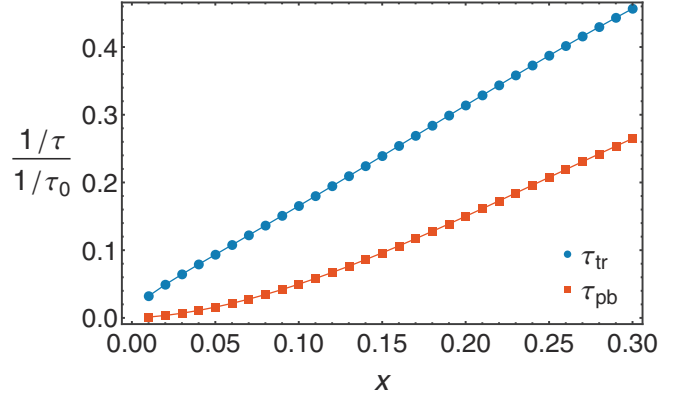


FIG. 1. Pair-breaking and transport scattering rates normalized by the noncorrelated value $1/\tau_0$ as a function of the doping level.

dominated by the x^2 dependence of Eq. (6). Indeed, in the whole range of dopings from ~ 0.01 to ~ 0.3 , the product of the effective mass m^* and the angular integral in Eq. (6) varies very little (roughly from 5 to 3). Thus, in a manner very reminiscent of the strong healing of gap fluctuations found in Ref. [24], here the robustness of T_c can also be attributed to Mottness.

Transport scattering rate. The normal state resistivity is governed by the impurity induced transport scattering rate, which can be evaluated straightforwardly via Eq. (3) to give (see Supplemental Material [30])

$$\frac{1}{\tau_{tr}} = \frac{xn m^*}{2\pi} \int_0^{2\pi} d\theta g\left[\left|\sin\left(\frac{\theta}{2}\right)\right|\right] (1 - \cos \theta). \quad (11)$$

The noncorrelated transport scattering rate is defined as

$$\frac{1}{\tau_0} = \frac{nm}{2\pi} \int_0^{2\pi} d\theta t^2 (1 - \cos \theta), \quad (12)$$

which coincides with the above $1/\tau_0$ for the bare isotropic scattering impurity potential we used. As shown in Fig. 1, the transport rate is also suppressed by electronic correlations and Mottness. In contrast to Eq. (6), however, the dependence is almost linear in x . This is because, as before, the product of m^* and the angular integral in Eq. (11) is almost doping independent. As a result, as seen in Fig. 1, for a wide range of doping levels the suppression of the pair-breaking scattering rate is much more significant than the transport one.

Forward scattering. The doping dependence of the scattering rates illustrated in Fig. 1 makes it clear that the dominant effect comes from the explicit x dependence in Eqs. (6) ($\sim x^2$) and (11) ($\sim x$). The x dependence coming from m^* times the angular integrals over the scattering matrices is very weak. However, this does not mean that the angular dependence of the T matrices is not affected by strong correlations, as we will now show.

In Fig. 2 we show, for two doping levels, the angular dependence of the function $g[\left|\sin(\frac{\theta}{2})\right|]$ [defined in Eq. (7)], which is integrated over in Eqs. (6) and (11). This should be compared to the bare impurity result, which is $\sim t^2$ and thus θ independent. Clearly, there is a large enhancement of forward scattering, indicating a “softening” of the impurity scattering by correlations, even for pointlike impurities in the plane.

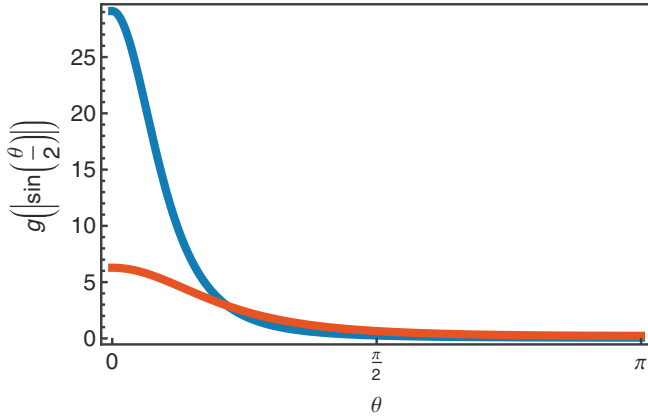


FIG. 2. Angular dependence of the renormalized T matrices at $x = 0.15$ (blue) and $x = 0.3$ (red).

This function is weighted by $1 - \cos 2\theta$ and $1 - \cos \theta$ in the integrations in Eqs. (6) and (11), respectively. These weight functions amplify the contributions from the regions $\theta \approx \pi/2$ and $\theta \approx \pi$, respectively, which are, however, hardly affected

by correlations. As a result, even with the softening of the impurity scattering, the angular integrals are not renormalized significantly in the range from ~ 0.15 to ~ 0.3 , when compared to the noncorrelated bare impurity result: ~ 0.8 – 1 in Eq. (6) and ~ 0.3 – 0.5 in Eq. (11). The conclusion, then, is that strong correlations enhance significantly the forward scattering region even for pointlike in-plane impurities, but this is *not* the reason for the robustness of T_c or the resilience of the normal state conductivity.

Conclusions. We have shown how the weak-coupling AG theory of T_c suppression and normal state resistivity by dilute nonmagnetic impurities is modified in a strongly correlated metal. Even though the renormalized scattering amplitude is strongly enhanced in the forward direction, the most significant effect comes from the suppression of the electron fluid compressibility by Mottness, which is effective even relatively far from the Mott insulating state. Given its simplicity, we suggest that this phenomenon is generic to other systems close to Mott localization.

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